

Anonymous and Transparent Gateway-based Authenticated Key-Exchange

Michel Abdalla, Malika Izabachène et David Pointcheval

École Normale Supérieure (Paris)

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Key Exchange Protocol

A fundamental problem in cryptography: enable secure communication over insecure channels

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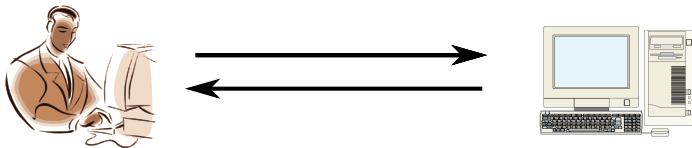
A fundamental problem in cryptography: enable secure communication over insecure channels

A common scenario: Users encrypt and authenticate their messages using a shared secret

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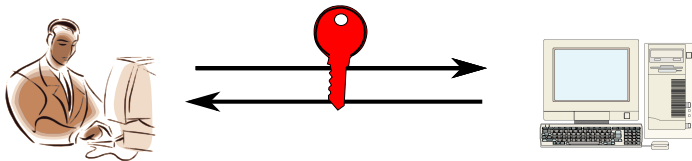
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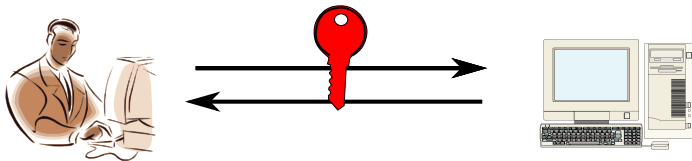
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How to share a secret key?

Key-exchange protocol

Diffie-Hellman protocol [DH76] (1/2)

\mathbb{G} is group where the CDH problem is hard to solve
 g a public generator of \mathbb{G}

The CDH Problem:

Given g , g^x et g^y , compute g^{xy}
(x and y are private)

The DDH problem:

Given g , g^x , g^y et z , decide whether $z \stackrel{?}{=} g^{xy}$
(x and y private)

Diffie-Hellman Protocol [DH76] (2/2)

\mathbb{G} is a group where the CDH problem is hard to solve
 g a public generator of \mathbb{G}

Alice

Bob

$$sk_A \xleftarrow{R} \{0, \dots, |\mathbb{G}| - 1\}$$

$$pk_A = g^{sk_A}$$

$$\xrightarrow{pk_A} sk_B \xleftarrow{R} \{0, \dots, |\mathbb{G}| - 1\}$$

$$\xleftarrow{pk_B} pk_B = g^{sk_B}$$

The common secret key is $sk = pk_B^{sk_A} = g^{sk_A sk_B} = pk_A^{sk_B}$

Problem: this scheme is not authenticated

Both Alice and Bob don't know to whom they are actually speaking

Authenticated Key Exchange (AKE)

Allow two parties to establish a common session key
→ in an authenticated manner

- **Intuitive Goal:** provides implicit authentication
The session key should be known to the involved parties
- **Formal Modelisation:** provides Semantic Security of the key
The session key should be indistinguishable from a random string

Forward-secrecy: even if a long-term secret is exposed (in the future), the security of the current session key is preserved.

Diffie-Hellman: a *man-in-the-middle* is possible
→ no authentication is possible

Authentication Techniques

- Asymmetric Techniques

We assume the existence of a PKI (*public-key infrastructure*).
Each user owns a pair (secret key, public key) given to him by a trusted authority

- Symmetric Techniques

Users share a random secret key

- Password-Based Techniques

Users shares a low-entropy secret key

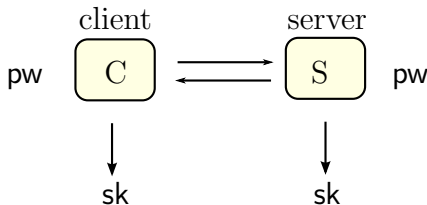
Example: about 4-digits pincode, a ssh password

→ Password-Based authentication

Outline

- 1 Password-Based Key Exchange Protocol
- 2 Security Model
- 3 Notion of Gateway-Based PAKE
- 4 Strengthening the Security Model
- 5 Sketch of the Proof
- 6 Client Anonymty

Password-Based AKE



✓ **Realistic:**

Real life applications actually rely on weak passwords

✓ **Convenient to use:**

Users do not need to store the secret

✗ **But subject to online dictionary attacks:** Unavoidable attacks
(small size of the dictionary)

Online Dictionary Attacks

Let D be the set of all possible passwords (*dictionary*)
from which are drawn random passwords $\rightarrow |D|$ is small

Online dictionary attacks:

- choose a password in D
- interact with the authentication server using pw
- each attempt can succeed with probability $1/|D|$

Protection against these attacks:

limit the number of failed attempts

Aim of the password-based authentication:

restrict the adversary to these attacks only

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Communication Model

The users can have several instances running concurrently (U^i for a user and S^j for a server in the two-party case)

- Each user will be associated to an oracle instance
- The i_{th} instance of player U will be called U^i

Communication can be controlled by the adversary (\mathcal{A}):

- Insecure channels: \mathcal{A} can create, forward or cancel messages
- Flows can be modified or dropped by \mathcal{A}
- Message transmission is done *via* specific queries to the oracles

Adversary's queries (1/3)

- $\text{Execute}(U^i, S^j)$
→ \mathcal{A} obtains the *transcript* of the execution
Models passive attacks (*eavesdropping*) on an execution of the protocol between U^i et S^j
- $\text{Reveal}(U^i)$
→ \mathcal{A} obtains the established session key of U^i
Models a misuse of the session key by U^i
- $\text{Send}(U^i, m)$
→ \mathcal{A} sends the message m to U^i
Models an active attacks against U^i
- $\text{Test}(U^i)$
→ \mathcal{A} obtains U^i 's session key if $b = 0$ or a random session key if $b = 1$
Models the semantic security of U^i 's session key

Adversary's queries (2/2)

Notion of partnering:

- two instances are partnered if they share the same *sid*
- in the standard model, $sid = transcript$ of the session
- the probability that two instances share the same *sid* is negligible

Freshness:

- a player instance is fresh if it has accepted the session key session and if no Reveal query has been asked to it or its partner
- a Test query is forbidden on a non-fresh instance
- the freshness status allows to remove trivial attacks against semantic security

Notions of Security

Advantage of the adversary:

$$\text{Adv}_P^{\text{ake}}(t, q_{\text{reveal}}, q_{\text{send}}, q_{\text{execute}}) = \max_{\mathcal{A}}(2\Pr(\text{Succ}) - 1)$$

- Succ is the event for which \mathcal{A} guesses the bit involved in a Test query correctly
- q_{reveal} , q_{send} et q_{exe} are the maximum number of queries \mathcal{A} has done to Reveal, Send and Execute oracle.

A PAKE is secure if: $\text{Adv}_P^{\text{ake}} \approx q_{\text{send}}/|D| + \text{negl}(k)$

$q_{\text{send}}/|D|$: online Dictionary attacks

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Extension to the Three party case



Client

pw



Server

pw

Extension to the Three party case



Client

pw



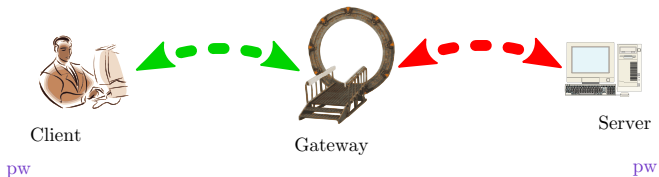
Gateway



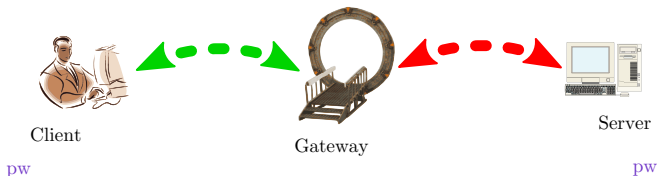
Server

pw

Extension to the Three party case



Extension to the Three party case



Motivation for GPAKE:

- Practical situation: the authentication task is left to different entities
- Security against off-line Dictionary Attacks is not enough (w.r.t malicious gateway)

Model for GPAKE

Our goal:

- 1 the Gateway doesn't learn anything about the password

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Guarantee Semantic Security of the session key

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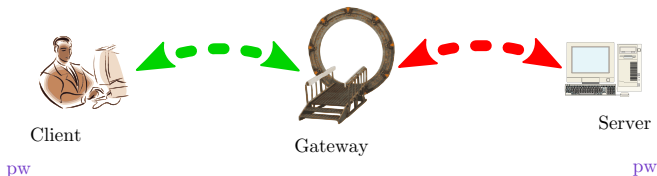
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Guarantee Semantic Security of the session key

- 3 Mutual Authentication: the Client and the Gateway are both sure to speak to each other

Both compute the real session key with its actual partner

Gateway-Based PAKE [ACFP05]



$$\begin{array}{l}
 \text{PW} = \\
 \mathcal{G}(C, S, \text{pw}) \\
 \in D \subset \mathbb{G}
 \end{array}
 \begin{array}{c}
 \xrightarrow{\text{(flow1)}} \\
 \xleftarrow{\text{(flow4)}}
 \end{array}$$

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Our contributions for the model

- **A Unified Security Model:** consider semantic security and unilateral (resp. mutual) authentication simultaneously
- **Stronger Notion of Corruption:** even if participants are corrupted (leakage of a long-term secret), the session can remain *fresh*
 - this allows to consider a stronger notion of perfect forward-secrecy
- **Client Anonymity w.r.t the Server:** The Server doesn't know which Client is currently connected
 - strengthen the Transparency property

More Fresh sessions

Idea: specify the identity of the sender of a Send query

A session is fresh if

- 1 instances involved have accepted and nobody is corrupted and no Reveal query has been asked (as before)
- 2 all (or some of) messages are oracle generated

→ even if a participant is corrupted, the session could be maintained as fresh

Tools for GPAKE

A Diffie-Hellman-Based Assumption: PCDDH

Password chosen basis Diffie-Hellman Assumption

- 1 Round 1: give D to \mathcal{A}
 \mathcal{A} returns a basis X
- 2 Round 2: choose $s_0, s_1 \xleftarrow{\mathcal{R}} \mathbb{Z}_q$ and $PW \in D$
choose $b \in \{0, 1\}$
set $X' \leftarrow (X/PW)^{s_b}$ and $Y \leftarrow g^{s_1}$
- 3 Round 3: Given Y and X'
 \mathcal{A} returns his response b' for b

Interactive assumption but ...

quite reasonable assuming DDH holds (if pw is drawn uniformly at random in D)

Gateway-Based PAKE

client PW



server PW



Gateway-Based PAKE

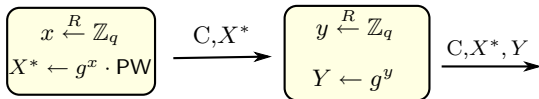


Gateway-Based PAKE

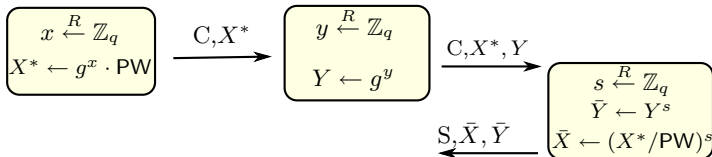


$$\begin{array}{l} x \xleftarrow{R} \mathbb{Z}_q \\ X^* \leftarrow g^x \cdot \text{PW} \end{array} \xrightarrow{C, X^*}$$

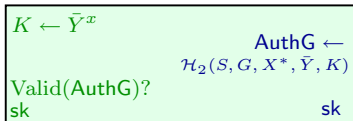
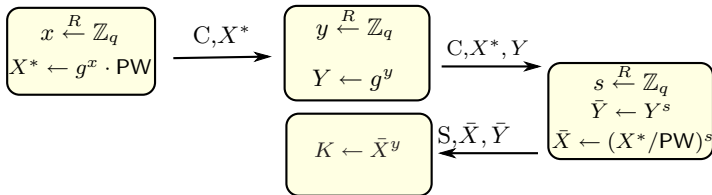
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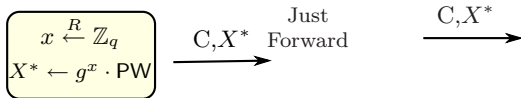
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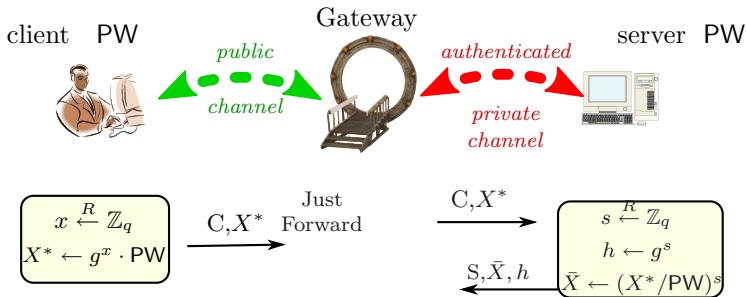
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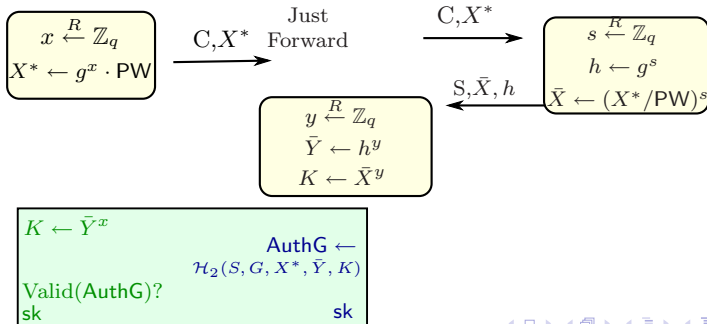
Anonymous Gateway-Based PAKE



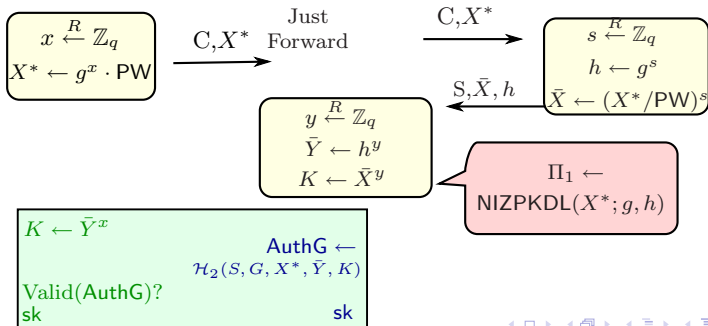
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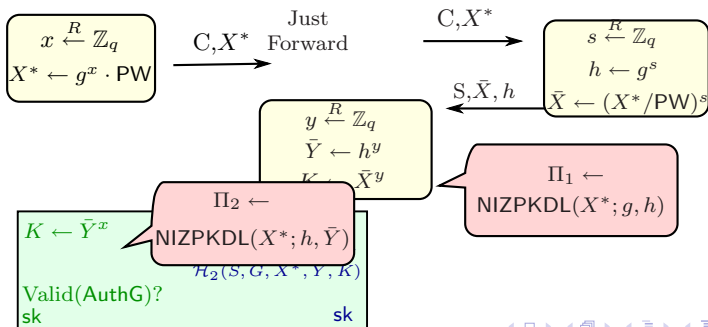
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Key Point of the Proof

General Idea: simulate oracle s.t. \mathcal{A} 's view is negligibly close to the one in the real game

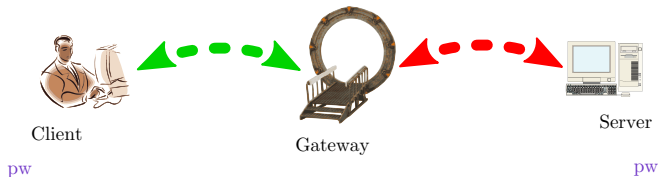
- Nobody is corrupted and \mathcal{A} interacts *passively* (OG or Execute) with the protocol
→ The semantic security relies on the CDH Problem
- If the Gateway is corrupted ?
- If the Client is corrupted ?
- Everybody is corrupted but the all messages are OG?

Trick in the proof (1/4)

More intricate case: the Gateway is corrupted

Trick in the proof (1/4)

More intricate case: the Gateway is corrupted



Trick in the proof (1/4)

More intricate case: the Gateway is corrupted

- 1 \mathcal{A} asks the help of the server

But the server oracle still uses PW

→ make sure that Dictionary attacks are not possible

- 2 \mathcal{A} plays on the behalf of the server and the gateway.

reject non-oracle generated authenticators

→ compute the probability of bad rejection

Trick in the proof (2/4)

Case 1: \mathcal{A} plays with a server oracle

→ use the **PCDDH** assumption to reduce \mathcal{A} 's task in deciding whether (g, h, \bar{X}) is **real or random**

if \mathcal{A} do so, we have an adversary against the PCDDH Assumption

How?

prove it by an hybrid argument on the number of q_{send} queries to the Server

Trick in the proof (3/4)

Case 2: \mathcal{A} plays on the behalf of the server and the gateway

we assume as symmetric authentication means b.t G and S

→ reject non oracle generated authenticators

can we detect it?

YES

Probability of Bad rejection?

Negligible if the client is not corrupted

Trick in the proof (4/4)

- Note that $(g, X^*/PW, h, \bar{X})$ is a CDH-tuple for at most one PW
- Goal of the simulation: Not use the password anymore

→ Goal: show that $P_1 = \frac{q_{send}}{N}$

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Adding Client Anonymity

The client may want to obtain a session key without letting the server know who he is

→ make the Client connections anonymous and unlikable

A Solution

- The Server is viewed as a dynamic database
- For each connection, construct all possible answers for the Client
- The Gateway gets the one for the Client

Adding Client Anonymity/Interface with a PIR

Feature of our GPAKE variant: can be efficiently interfaced with any *Private Information Retrieval*

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PIR problematic: allow a user to retrieve an item in a database (of size n) without letting know the server which index is asked

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Necessity of duplication of databases that do not collude

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- **Computational:** one database is possible [KO97]
Counterpart: more computational cost

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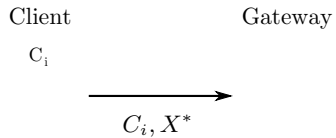
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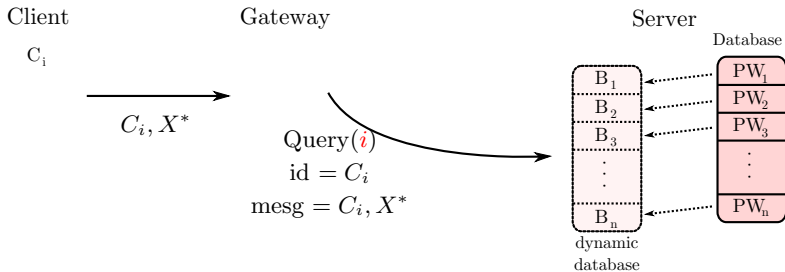
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Symmetrical PIR: Prevents user from learning more than one item of the database during a session [KO97, GIKM98]

Adding Client Anonymity



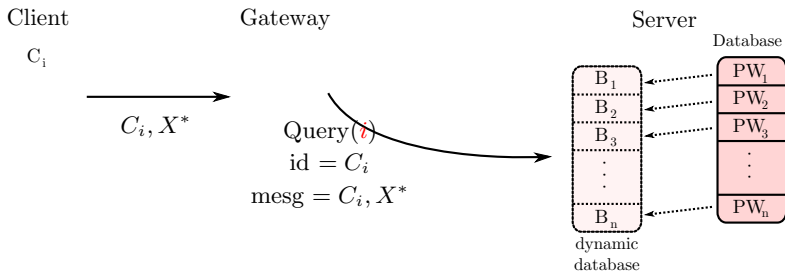
Adding Client Anonymity



$$B_i = (g^{s_i}, (X^*/PW_i)^{s_i}, \Pi_i)$$

$s_i \xleftarrow{R} \mathbb{Z}_q$

Adding Client Anonymity



Once for all: $h = g^s, \Pi_1, s \xleftarrow{R} \mathbb{Z}_q$

$$B_i = (X^*/PW_i)^s$$

- improve computational cost
- improve storage space

Conclusion

- Formalisation of a strengthened model for PAKE protocols considering a broader notion of Freshness
- Apply it to GPAKE
But still makes sense for the two-party case
→ lead to a (partial) mechanization of the proof (we only consider weak and static corruption)
- Suggest Client Anonymity

Open Question:

- Deal with Dynamic corruption
- Consider other distribution for the Dictionary than a uniform one